

Volume 1, Issue 1

Number of issues per year: 6

International Journal of Scientific and Statistical Computing (IJSSC)

ISSN : 2180-1339

**INTERNATIONAL JOURNAL OF
SCIENTIFIC AND STATISTICAL
COMPUTING (IJSSC)**

Volume 1, Issue 1, 2010

Edited By
Computer Science Journals
www.cscjournals.org

INTERNATIONAL JOURNAL OF SCIENTIFIC AND STATISTICAL COMPUTING (IJSSC)

Book: 2010 Volume 1, Issue 1

Publishing Date: 20-12-2010

Proceedings

ISSN (Online): 2180 -1339

This work is subjected to copyright. All rights are reserved whether the whole or part of the material is concerned, specifically the rights of translation, reprinting, re-use of illustrations, recitation, broadcasting, reproduction on microfilms or in any other way, and storage in data banks. Duplication of this publication of parts thereof is permitted only under the provision of the copyright law 1965, in its current version, and permission of use must always be obtained from CSC Publishers. Violations are liable to prosecution under the copyright law.

IJSSC Journal is a part of CSC Publishers

<http://www.cscjournals.org>

© IJSSC Journal

Published in Malaysia

Typesetting: Camera-ready by author, data conversion by CSC Publishing Services – CSC Journals, Malaysia

CSC Publishers

EDITORIAL PREFACE

The International Journal of Scientific and Statistical Computing (IJSSC) is an effective medium for interchange of high quality theoretical and applied research in Scientific and Statistical Computing from theoretical research to application development. This is the first issue of volume first of IJSSC. International Journal of Scientific and Statistical Computing (IJSSC) aims to publish research articles on numerical methods and techniques for scientific and statistical computation. IJSSC publish original and high-quality articles that recognize statistical modeling as the general framework for the application of statistical ideas.

Submissions reflect the important developments, extensions, and applications in statistical modeling. IJSSC goal is to be multidisciplinary in nature, promoting the cross-fertilization of ideas between scientific computation and statistical computation. IJSSC is refereed journal and invites researchers, practitioners to submit their research work that reflect new methodology on new computational and statistical modeling ideas, practical applications on interesting problems which are addressed using an existing or a novel adaptation of an computational and statistical modeling techniques and tutorials & reviews with papers on recent and cutting edge topics in computational and statistical concepts.

IJSSC editors understand that how much it is important for authors and researchers to have their work published with a minimum delay after submission of their papers. They also strongly believe that the direct communication between the editors and authors are important for the welfare, quality and wellbeing of the Journal and its readers. Therefore, all activities from paper submission to paper publication are controlled through electronic systems that include electronic submission, editorial panel and review system that ensures rapid decision with least delays in the publication processes.

To build international reputation of IJSSC, we are disseminating the publication information through Google Books, Google Scholar, Directory of Open Access Journals (DOAJ), Open J Gate, ScientificCommons, Docstoc, Scribd, CiteSeerX and many more. Our International Editors are working on establishing ISI listing and a good impact factor for IJSSC. I would like to remind you that the success of the journal depends directly on the number of quality articles submitted for review. Accordingly, I would like to request your participation by submitting quality manuscripts for review and encouraging your colleagues to submit quality manuscripts for review.

One of the great benefits that IJSSC editors provide to the prospective authors is the mentoring nature of the review process. IJSSC provides authors with high quality, helpful reviews that are shaped to assist authors in improving their manuscripts.

Editorial Board Member

International Journal of Scientific and Statistical Computing (IJSSC)

Editorial Board Members (EBMs)

Dr. De Ting Wu

Morehouse College (United States of America)

Table of Content

Volume 1, Issue 1, December 2010

Pages

- 1-6 Group Testing with Test Errors Made Easier
Nyongesa L. Kennedy, Paul J. Syaywa

Group Testing With Test Errors Made Easier

Nyongesa L. Kennedy

*Department of Mathematics,
Masinde Muliro University of Science and Technology,
190 kakamega, Kenya*

knyongesa@hotmail.com

Paul J. Syaywa

*Department of Mathematics
Masinde Muliro University of Science and Technology,
190 kakamega, Kenya
Research Partially Supported by MMUST-URF*

syaywa@yahoo.com

Abstract

Group testing is a cost-effective procedure for identifying defective items in a large population. It also improves the efficiency of the testing procedure when imperfect tests are employed. This study develops computational group-testing strategy based on [5] testing strategy. Statistical moments based on this applied design have been generated. With advent of digital computers in 1980's, group-testing strategy under discussion is handled in the context of computational statistics.

Keywords: False-negative; False-positive; Group; Imperfect-tests; Pool.

1. INTRODUCTION

Sequential testing of a population in the form of grouped sample started the way back in the second world war by [2] as a cost-effective method for screening syphilis in US soldiers returning from abroad. The [2] idea entails putting together individuals to form a group, and then testing the group rather than testing each individual for evidence or absence of the characteristic of interest. Epidemiological studies that use group testing have one of the two objectives. The first objective is to screen a large population with a view to identifying those individuals with a trait (cf. [2]). The second objective is to estimate the rate of the trait (cf. [10] and [9]). For either objective, group testing is more cost effective than individual testing especially when the rate of the trait is low because if a group tests negative it implies that none of the individuals that constitute the group have the trait, and thus it is not necessary to test each individual in the group.

In recent years, there has been renewed interest in group testing strategies of biological specimens because of the application in HIV/Aids epidemiology (cf. [5]). The procedure has potential in the application of HIV/Aids testing because disease prevalence is estimated without necessarily identifying the subject (cf. [3]). [12] studied the cost-effectiveness of pooling algorithm

for the first objective of identifying individuals with the trait. In their procedure, each individual group that test positive is divided into two equal groups, which are then tested. Groups that tested positive were further sub-divided and tested and so on. [13] extended this work by considering pooling algorithms when there are errors and showed that some of these algorithms can reduce the error rates of the screening procedures (the false positives and false negatives) compared to individual testing. [7] examined group testing with re-testing and observed that re-test improves the sensitivity and specificity of the group-testing algorithm.

Recent studies have focused on the second objective of estimating the rate of the trait using group-testing strategy. [11] discussed the procedure as a potential method for use by pharmaceutical companies in discovering drugs in the early stages. [8] has proposed an estimator in pool testing strategy that benefit from re-testing the pools. He observed that re-testing improves the efficiency of the estimator.

In this study, we discuss the computation of statistical measures in pool testing strategy with imperfect test via computer package MATLAB based on [5] design of pool testing strategy. To the authors knowledge no article has appeared in the literature of group-testing as championed by [2] that has discussed the procedure in computational aspect. The rest of the paper is arranged as follows: Group testing strategy with imperfect test or in the presence of test errors is introduced in Section 2. Various statistical moments are generated in Section 3. Misclassification in the proposed algorithm as a result of test errors is discussed in Section 4. Section 5 provides the conclusion to the present study.

2. THE TESTING STRATEGY

In this study, we generalize the group testing strategy by introducing the error component in the testing scheme so that the earlier proposed strategies become special cases as proposed by [5]. The strategy proposed in this study is as follows. Initially, group the population under investigation into a single group of size n and carry out a test on the group. If the test result is negative, further testing is discontinued. If the test result is positive, the group is divided into groups of equal sizes (nk), and each group is subjected to group-testing. If the group tests positive, individual testing is carried out. Diagrammatic description of the procedure has been presented in Figure 1.

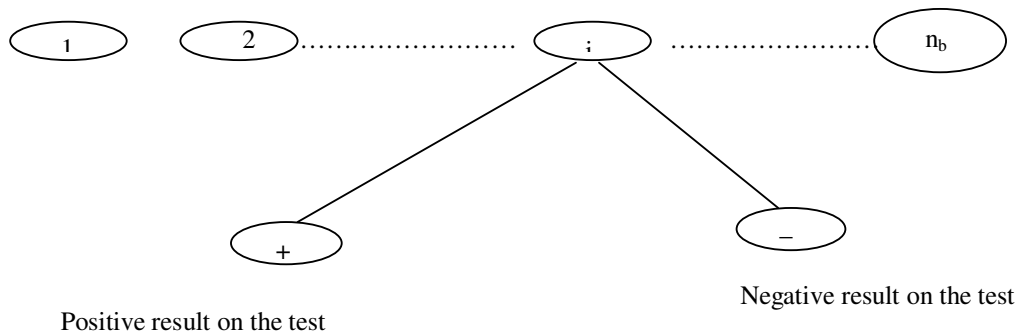


FIGURE 1: Block Testing Strategy

3. MOMENTS IN THE GROUP TESTING STRATEGY

Generation of random numbers from distributions form a basis for generation of moments in this section. Notice that, in order to use a computer to initiate a simulation study, we must be able to generate the values of a uniform (0,1) random variables; such variates are called random numbers, most computers have in-built subroutines, called a random number generator. For further discussion on this subject see [6].With the above in mind, we are in a position to generate moment measures in our proposed group testing strategy. In our testing strategy, we shall assume that tests under use are imperfect so that when tests are assumed to be perfect would be a special case. Before the generation of moments, we shall require the composite probability of classifying a group as positive, denoted by π and given by

$$\pi = (1 - (1 - p)^k)\phi + (1 - p)^k(1 - \psi) \tag{1}$$

where k is the group size, p is the probably of incidence, ϕ and ψ are the sensitivity and specificity of the test in use, respectively. Equation (1) is easily derived by the law of total probability. In our study, (1) is the probability of success. Therefore, we shall generate random numbers from a binomial distribution with probability of success π . Now, with (1) at hand, to convert the data set $\{x_i\}$ generated from $U(0, 1)$ into zeros and ones, we use the indicator function

$$x_i = \begin{cases} 1 & \text{if } x_i < \pi \\ 0 & \text{if } x_i \geq \pi \end{cases}$$

But from (1), it is clear that $0 \leq \pi \leq 1$ since $p \in (0, 1)$ and $\phi \leq 1$ and $\psi \leq 1$.

Also, notice that in situations where the test kits are perfect, $\phi = \psi = 1$. Then (1)

reduces to

$$\pi = 1 - (1 - p)^k \tag{2}$$

and if the group size is one, i.e., $k = 1$, (1) reduces to

$$\pi = p\phi + (1 - \psi)(1 - p) \tag{3}$$

Let X denote the number of defective groups (groups that test positive on the test), then $X \sim \text{binomial}(n, \pi)$. Hence, various statistical measures; mean, standard deviation, Kurtosis and skewness have been computed by the aid of statistical packages. In addition, the total numbers of tests, cost, and relative savings have been computed. We utilize Equations (1) and (3) to generate these moments as presented in Tables 1a (i), 1a(ii), 1a (iii), though 2(b). Graphical presentations are provided in Figures2(a) through 2(c) in the Appendix.

The simulation at population size 100 with groups of size 10 when the sensitivity and specificity of the tests in use are 99% is provided in Table 1(a)(i). It can be observed from the simulated results that:

- The numbers of defectives increase with increase in the incidence probability p
- The number of tests increases with increase in p,
- Relative savings decrease with increase is p.

If the population size is increased to 500 or 1000 from 100 with group size 20, as presented in Tables 1a(ii) and 1a(iii), respectively, similar observations are made as noted above. Further, notice that when the population size is fixed but the group size is increased, more defectives are realized but there is no significant difference in relative savings. This is noted when we compare Table 1a(ii) and Table 1a(iii).

Now, varying the sensitivity and specificity from 99% to 95% as provided by Tables 1 b(i) to 1 b(iii), we draw similar conclusion. Graphical evidence of the observations on average number of tests required to identify all defective items in the group is provided by Figures 2(a) through 2(c). Clearly, the observations made are true in practice. Group testing strategy is only visible when the incidents probability is small [2]. Otherwise individual testing is preferred. Thus, the tables provides empirical evidence of the group testing scheme.

4. MISCLASSIFICATIONS IN GROUP TESTING STRATEGY

Our main assumption in the discussion of this study was that test act independently and errors are part of the design as it is the case in practice ([7],[1]). Thus, misclassifications are bound to arise in the testing scheme. There are two possible misclassifications in the literature of group-testing namely:

- A defective item is classified as non-defective and termed as false negative,
- A non-defective item classified as defective, false positive.

The probabilities of interest here are the probability of false positive

$$f_p = 1 - \phi^2 \tag{4}$$

and the probability of false negative is

$$f_n = 1 - (1 - (1 - p)^{k-1})[1 - \phi + \phi\psi] - (1 - p)^{k-1}[\psi(1 - \psi) + \psi] \tag{5}$$

We now utilize (4) and (5) to compute misclassifications as presented in Tables 3(a), 3(b),3(c), and 3(d). The simulated results are also presented graphically in Figures 3(a), 3(b), 3(c) and 3(d). Computed values of false positives for group sizes:100, 500, 1000 with group sizes of 10, 20, and 50 have been presented in Table 3(a) and 3(b), when tests with equal sensitivity and specificity are employed. It can be observed that:

- The number of false positive increases with increase in p,
- More false positives are realized with increase in group size. In fact, when the group size is

doubled,

false positive increase by at least two fold,

- Increase in the efficiency of the test kits results into a reduction in false positives.

From Tables 3(c) and 3(d), we observe that:

- The number of false-negative increase at a slow rate with increase in the incidence probability,
- The number of false negatives approximately doubles when the group size is doubled,
- If the efficiency of the tests is increased, fewer false negatives are realized.

5. CONCLUSION

We have presented a computational pool testing strategy with test errors based on [5] design. It is evident from the computed results; Tables 1 (a)I to 1 (a) iii, that groups should be relatively small to be able to obtain the desired results as relative savings decrease with increase in pool sizes. This observation is feasible in situations where dilution effect can affect the results (cf. [4]). Also notice that relative savings is prominent when the efficiency of the test kits are high. Furthermore, the computed results support the idea that the procedure is only feasible when the prevalence rate is small otherwise individual testing is preferable. i.e relative savings decrease with increase in prevalence rate. Misclassifications are prominent when the efficiency of the test kits are low and incidence probability high, calling for re-testing, [7] and [8].

6. REFERENCES

1. R. Brookmeyer. ``*Analysis of multistage pooling studies of Biological specimens for Estimating Disease Incidence and prevalence*``. Biometric 55, 608-612, 1999.
2. R. Dorfman. ``*The Detection of Defective Members of Large Population*``. Annals of Mathematical Statistics 14, 436-440, 1943.
3. J.L.Gastwirth, P.A. Hammick. ``*Estimation of the prevalence of a Rare Disease, Preserving the Anonymity of the Subject by group-Testing; Application to Estimating the Prevalence of AIDS Antibodies in Blood Donor*``.Journal of Statistical Planning and Inference 22, 15-27, 1989.
4. F.K. Hwang. ``*Group Testing with a Dilution Effect*``. Biometrika 63, 611-613, 1975.
5. R.L. Kline, T. Bothus, R. Brookmeyer, S.Zeyer, T. Quinn.``*Evaluation of Human Immunodeficiency Virus Sera Prevalence in Population Surveys Using Pooled Sera*``. Journal of Clinical Microbiology 27, 1449-145, 1989.
6. W.L.Martinez, A.R. Martinez, A.R. ``*Computational Statistics Handbook with MATLAB*``. Chapman & Hall/CRC, (2002).
7. L.K. Nyongesa. `` *Multistage group Testing Procedure (group Screening)*``.

Communications in Statistics-Simulation and Computation 33(3), 621-637, 2004.

- 8 L.K Nyongesa. ``Dual Estimation of Prevalence and Disease Incidence in Pool-Testing Strategy''.Communication in Statistics Theory and Method (in Press), 2010.
9. M. Sobel, R.M. Elashoff , R. M. (1975). ``Group-Testing with a New Goal, Estimation''. Biometrika 62, 181-193, 1975.
10. K.H.Thompson. ``Estimation of the Population of Vectors in a Natural Population of Insects''. Biometrics 18, 568-578, 1962.
11. M. Xie, K. Tatsuoka, J.Sacks, S.Young. ``Group testing with Blockers and synergism''. Journal of American Statistical Association 96, 92-101, 2001.
12. N.I. Johnson,S.Kotz, X. Wu. ``Inspection Errors for Attributes in Quality Control''. London: Chapman and Hall, (1991).
13. E. Litvak, X.M.Tu, M. Pagano.`` Screening for the Presence of Disease by Pooling Sera Samples''. Journal of the American Statistical Association, 89, 424-434, 1994.

CALL FOR PAPERS

Journal: International Journal of Scientific And Statistical Computing (IJSSC)

Volume: 2 **Issue:** 1

ISSN: 2180-1339

URL: <http://www.cscjournals.org/csc/description.php?JCode=IJSSC>

About IJSSC

International Journal of Scientific and Statistical Computing (IJSSC) aims to publish research articles on numerical methods and techniques for scientific and statistical computation. IJSSC publish original and high-quality articles that recognize statistical modeling as the general framework for the application of statistical ideas. Submissions must reflect important developments, extensions, and applications in statistical modeling. IJSSC also encourages submissions that describe scientifically interesting, complex or novel statistical modeling aspects from a wide diversity of disciplines, and submissions that embrace the diversity of scientific and statistical modeling.

IJSSC goal is to be multidisciplinary in nature, promoting the cross-fertilization of ideas between scientific computation and statistical computation. IJSSC is refereed journal and invites researchers, practitioners to submit their research work that reflect new methodology on new computational and statistical modeling ideas, practical applications on interesting problems which are addressed using an existing or a novel adaptation of an computational and statistical modeling techniques and tutorials & reviews with papers on recent and cutting edge topics in computational and statistical concepts.

To build its International reputation, we are disseminating the publication information through Google Books, Google Scholar, Directory of Open Access Journals (DOAJ), Open J Gate, ScientificCommons, Docstoc and many more. Our International Editors are working on establishing ISI listing and a good impact factor for IJSSC.

IJSSC List of Topics

The realm of International Journal of Scientific and Statistical Computing (IJSSC) extends, but not limited, to the following:

- Annotated Bibliography of Articles for the Statist
- Bibliography for Computational Probability and Sta
- Current Index to Statistics
- Guide to Statistical Computing
- Solving Non-Linear Systems
- Statistics and Statistical Graphics
- Theory and Applications of Statistics and Probabil
- Annals of Statistics
- Computational Statistics
- Environment of Statistical Computing
- Mathematics of Scientific Computing
- Statistical Computation and Simulation
- Symbolic computation

Important Dates

Volume: 1

Issue: 2

Paper Submission: November 30, 2010

Author Notification: January 01, 2011

Issue Publication: January / February 2011

CALL FOR EDITORS/REVIEWERS

CSC Journals is in process of appointing Editorial Board Members for **INTERNATIONAL JOURNAL OF SCIENTIFIC AND STATISTICAL COMPUTING (IJSSC)**. CSC Journals would like to invite interested candidates to join **IJSSC** network of professionals/researchers for the positions of Editor-in-Chief, Associate Editor-in-Chief, Editorial Board Members and Reviewers.

The invitation encourages interested professionals to contribute into CSC research network by joining as a part of editorial board members and reviewers for scientific peer-reviewed journals. All journals use an online, electronic submission process. The Editor is responsible for the timely and substantive output of the journal, including the solicitation of manuscripts, supervision of the peer review process and the final selection of articles for publication. Responsibilities also include implementing the journal's editorial policies, maintaining high professional standards for published content, ensuring the integrity of the journal, guiding manuscripts through the review process, overseeing revisions, and planning special issues along with the editorial team.

A complete list of journals can be found at <http://www.cscjournals.org/csc/byjournal.php>. Interested candidates may apply for the following positions through <http://www.cscjournals.org/csc/login.php>.

Please remember that it is through the effort of volunteers such as yourself that CSC Journals continues to grow and flourish. Your help with reviewing the issues written by prospective authors would be very much appreciated.

Feel free to contact us at coordinator@cscjournals.org if you have any queries.

Contact Information

Computer Science Journals Sdn Bhd

M-3-19, Plaza Damas Sri Hartamas
50480, Kuala Lumpur MALAYSIA

Phone: +603 6207 1607
 +603 2782 6991
Fax: +603 6207 1697

BRANCH OFFICE 1

Suite 5.04 Level 5, 365 Little Collins Street,
MELBOURNE 3000, Victoria, AUSTRALIA

Fax: +613 8677 1132

BRANCH OFFICE 2

Office no. 8, Saad Arcad, DHA Main Bulevard
Lahore, PAKISTAN

EMAIL SUPPORT

Head CSC Press: coordinator@cscjournals.org
CSC Press: cscpress@cscjournals.org
Info: info@cscjournals.org

COMPUTER SCIENCE JOURNALS SDN BHD
M-3-19, PLAZA DAMAS
SRI HARTAMAS
50480, KUALA LUMPUR
MALAYSIA