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Intuitionistic Fuzzy W- Closed Sets and Intuitionistic Fuzzy W -Continuity

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Abstract

The aim of this paper is to introduce and study the concepts of intuitionistic fuzzy w-closed sets, intuitionistic fuzzy w-continuity and intuitionistic fuzzy w-open & intuitionistic fuzzy w-closed mappings in intuitionistic fuzzy topological spaces.

Key words: Intuitionistic fuzzy w-closed sets, Intuitionistic fuzzy w-open sets, Intuitionistic fuzzy w-connectedness, Intuitionistic fuzzy w-compactness, intuitionistic fuzzy w-continuous mappings.

2000, Mathematics Subject Classification: 54A

1. INTRODUCTION

After the introduction of fuzzy sets by Zadeh [23] in 1965 and fuzzy topology by Chang [4] in 1967, several researches were conducted on the generalizations of the notions of fuzzy sets and fuzzy topology. The concept of intuitionistic fuzzy sets was introduced by Atanassov [1] as a generalization of fuzzy sets. In the last 25 years various concepts of fuzzy mathematics have been extended for intuitionistic fuzzy sets. In 1997 Coker [5] introduced the concept of intuitionistic fuzzy topological spaces. Recently many fuzzy topological concepts such as fuzzy compactness [7], fuzzy connectedness [21], fuzzy separation axioms [3], fuzzy continuity [8], fuzzy g-closed sets [15] and fuzzy g-continuity [16] have been generalized for intuitionistic fuzzy topological spaces. In the present paper we introduce the concepts of intuitionistic fuzzy w-closed sets; intuitionistic fuzzy w-open sets, intuitionistic fuzzy w-connectedness, intuitionistic fuzzy w-compactness and intuitionistic fuzzy w-continuity obtain some of their characterization and properties.

2. PRELIMINARIES

Let X be a nonempty fixed set. An intuitionistic fuzzy set $A[1]$ in X is an object having the form $A = \{ \langle x, \mu_A(x), \gamma_A(x) \rangle : x \in X \}$, where the functions $\mu_A : X \rightarrow [0,1]$ and $\gamma_A : X \rightarrow [0,1]$ denotes the degree of membership $\mu_A(x)$ and the degree of non membership $\gamma_A(x)$ of each element $x \in X$ to the set A respectively and $0 \leq \mu_A(x) + \gamma_A(x) \leq 1$ for each $x \in X$. The intuitionistic fuzzy sets $\tilde{0} = \{ \langle x, 0, 1 \rangle : x \in X \}$ and $\tilde{1} = \{ \langle x, 1, 0 \rangle : x \in X \}$ are respectively called empty and whole intuitionistic fuzzy set on X . An intuitionistic fuzzy set $A = \{ \langle x, \mu_A(x), \gamma_A(x) \rangle : x \in X \}$ is called a subset of an intuitionistic fuzzy set $B = \{ \langle x, \mu_B(x), \gamma_B(x) \rangle : x \in X \}$ (for short $A \subseteq B$) if $\mu_A(x) \leq \mu_B(x)$ and $\gamma_A(x) \geq \gamma_B(x)$ for each $x \in X$. The complement of an intuitionistic fuzzy set $A = \{ \langle x, \mu_A(x), \gamma_A(x) \rangle : x \in X \}$ is the intuitionistic fuzzy set $A^c = \{ \langle x, \gamma_A(x), \mu_A(x) \rangle : x \in X \}$. The intersection (resp. union) of any arbitrary family of intuitionistic fuzzy sets $A_i = \{ \langle x, \mu_{A_i}(x), \gamma_{A_i}(x) \rangle : x \in X, (i \in \Lambda) \}$ of X be the intuitionistic fuzzy set $\cap A_i = \{ \langle x, \wedge \mu_{A_i}(x), \vee \gamma_{A_i}(x) \rangle : x \in X \}$ (resp. $\cup A_i = \{ \langle x, \vee \mu_{A_i}(x), \wedge \gamma_{A_i}(x) \rangle : x \in X \}$). Two intuitionistic fuzzy sets $A = \{ \langle x, \mu_A(x), \gamma_A(x) \rangle : x \in X \}$ and $B = \{ \langle x, \mu_B(x), \gamma_B(x) \rangle : x \in X \}$ are said to be q -coincident ($A_q B$ for short) if and only if \exists an element $x \in X$ such that $\mu_A(x) > \gamma_B(x)$ or $\gamma_A(x) < \mu_B(x)$. A family \mathfrak{S} of intuitionistic fuzzy sets on a non empty set X is called an intuitionistic fuzzy topology [5] on X if the intuitionistic fuzzy sets $\tilde{0}, \tilde{1} \in \mathfrak{S}$, and \mathfrak{S} is closed under arbitrary union and finite intersection. The ordered pair (X, \mathfrak{S}) is called an intuitionistic fuzzy topological space and each intuitionistic fuzzy set in \mathfrak{S} is called an intuitionistic fuzzy open set. The complement of an intuitionistic fuzzy open set in X is known as intuitionistic fuzzy closed set. The intersection of all intuitionistic fuzzy closed sets which contains A is called the closure of A . It is denoted $cl(A)$. The union of all intuitionistic fuzzy open subsets of A is called the interior of A . It is denoted $int(A)$ [5].

Lemma 2.1 [5]: Let A and B be any two intuitionistic fuzzy sets of an intuitionistic fuzzy topological space (X, \mathfrak{S}) . Then:

- (a). $\overline{A_q B} \Leftrightarrow A \subseteq B^c$.
- (b). A is an intuitionistic fuzzy closed set in $X \Leftrightarrow cl(A) = A$.
- (c). A is an intuitionistic fuzzy open set in $X \Leftrightarrow int(A) = A$.
- (d). $cl(A^c) = (int(A))^c$.
- (e). $int(A^c) = (cl(A))^c$.
- (f). $A \subseteq B \Rightarrow int(A) \subseteq int(B)$.
- (g). $A \subseteq B \Rightarrow cl(A) \subseteq cl(B)$.
- (h). $cl(A \cup B) = cl(A) \cup cl(B)$.
- (i). $int(A \cap B) = int(A) \cap int(B)$.

Definition 2.1 [6]: Let X is a nonempty set and $c \in X$ a fixed element in X . If $\alpha \in (0, 1]$ and $\beta \in [0, 1)$ are two real numbers such that $\alpha + \beta \leq 1$ then:

- (a) $c(\alpha, \beta) = \langle x, c_\alpha, c_{1-\beta} \rangle$ is called an intuitionistic fuzzy point in X , where α denotes the degree of membership of $c(\alpha, \beta)$, and β denotes the degree of non membership of $c(\alpha, \beta)$.
- (b) $c(\beta) = \langle x, 0, 1 - c_{1-\beta} \rangle$ is called a vanishing intuitionistic fuzzy point in X , where β denotes the degree of non membership of $c(\beta)$.

Definition 2.2[7] : A family $\{ G_i : i \in \Lambda \}$ of intuitionistic fuzzy sets in X is called an intuitionistic fuzzy open cover of X if $\cup \{ G_i : i \in \Lambda \} = \tilde{1}$ and a finite subfamily of an intuitionistic fuzzy open cover $\{ G_i : i \in \Lambda \}$ of X which also an intuitionistic fuzzy open cover of X is called a finite sub cover of $\{ G_i : i \in \Lambda \}$.

Definition 2.3[7]: An intuitionistic fuzzy topological space (X, \mathfrak{S}) is called fuzzy compact if every intuitionistic fuzzy open cover of X has a finite sub cover.

Definition 2.4[8]: An intuitionistic fuzzy set A of an intuitionistic fuzzy topological space (X, \mathfrak{S}) is called intuitionistic fuzzy semi open (resp. intuitionistic fuzzy semi closed) if there exists a intuitionistic fuzzy open (resp. intuitionistic fuzzy closed) U such that $U \subseteq A \subseteq \text{cl}(A)$ (resp. $\text{int}(U) \subseteq A \subseteq U$)

Definition 2.5 [21]: An intuitionistic fuzzy topological space X is called intuitionistic fuzzy connected if there is no proper intuitionistic fuzzy set of X which is both intuitionistic fuzzy open and intuitionistic fuzzy closed .

Definition 2.6[15]: An intuitionistic fuzzy set A of an intuitionistic fuzzy topological space (X, \mathfrak{S}) is called:

- (a) Intuitionistic fuzzy g -closed if $\text{cl}(A) \subseteq O$ whenever $A \subseteq O$ and O is intuitionistic fuzzy open.
- (b) Intuitionistic fuzzy g -open if its complement A^c is intuitionistic fuzzy g -closed.

Remark 2.1[15]: Every intuitionistic fuzzy closed set is intuitionistic fuzzy g -closed but its converse may not be true.

Definition 2.7[18]: An intuitionistic fuzzy set A of an intuitionistic fuzzy topological space (X, \mathfrak{S}) is called:

- (a) Intuitionistic fuzzy sg -closed if $\text{scl}(A) \subseteq O$ whenever $A \subseteq O$ and O is intuitionistic fuzzy semi open.
- (b) Intuitionistic fuzzy sg -open if its complement A^c is intuitionistic fuzzy sg -closed.

Remark 2.2[18]: Every intuitionistic fuzzy semi-closed (resp. Intuitionistic fuzzy semi-open) set is intuitionistic fuzzy sg -closed (intuitionistic fuzzy sg -open) but its converse may not be true.

Definition 2.8[12]: An intuitionistic fuzzy set A of an intuitionistic fuzzy topological space (X, \mathfrak{S}) is called:

- (a) Intuitionistic fuzzy gs -closed if $\text{scl}(A) \subseteq O$ whenever $A \subseteq O$ and O is intuitionistic fuzzy open.
- (b) Intuitionistic fuzzy gs -open if its complement A^c is intuitionistic fuzzy gs -closed.

Remark 2.3[12]: Every intuitionistic fuzzy sg -closed (resp. Intuitionistic fuzzy sg -open) set is intuitionistic fuzzy gs -closed (intuitionistic fuzzy gs -open) but its converse may not be true.

Definition 2.9: [5] Let X and Y are two nonempty sets and $f: X \rightarrow Y$ is a function. :

- (a) If $B = \{ \langle y, \mu_B(y), \gamma_B(y) \rangle : y \in Y \}$ is an intuitionistic fuzzy set in Y , then the pre image of B under f denoted by $f^{-1}(B)$, is the intuitionistic fuzzy set in X defined by

$$f^{-1}(B) = \{ \langle x, f^{-1}(\mu_B)(x), f^{-1}(\gamma_B)(x) \rangle : x \in X \}.$$

- (b) If $A = \{ \langle x, \lambda_A(x), \nu_A(x) \rangle : x \in X \}$ is an intuitionistic fuzzy set in X , then the image of A under f denoted by $f(A)$ is the intuitionistic fuzzy set in Y defined by

$$f(A) = \{ \langle y, f(\lambda_A)(y), f(\nu_A)(y) \rangle : y \in Y \}$$

Where $f(\nu_A) = 1 - f(1 - \nu_A)$.

Definition 2.10[8]: Let (X, \mathfrak{S}) and (Y, σ) be two intuitionistic fuzzy topological spaces and let $f: X \rightarrow Y$ be a function. Then f is said to be

- (a) Intuitionistic fuzzy continuous if the pre image of each intuitionistic fuzzy open set of Y is an intuitionistic fuzzy open set in X .
- (b) Intuitionistic fuzzy semi continuous if the pre image of each intuitionistic fuzzy open set of Y is an intuitionistic fuzzy semi open set in X .
- (c) Intuitionistic fuzzy closed if the image of each intuitionistic fuzzy closed set in X is an intuitionistic fuzzy closed set in Y .
- (d) Intuitionistic fuzzy open if the image of each intuitionistic fuzzy open set in X is an intuitionistic fuzzy open set in Y .

Definition 2.6[12, 16,17 19]: Let (X, \mathfrak{S}) and (Y, σ) be two intuitionistic fuzzy topological spaces and let $f: X \rightarrow Y$ be a function. Then f is said to be

- (a) Intuitionistic fuzzy g -continuous [16] if the pre image of every intuitionistic fuzzy closed set in Y is intuitionistic fuzzy g -closed in X .
- (b) Intuitionistic fuzzy gc -irresolute[17]if the pre image of every intuitionistic fuzzy g -closed in Y is intuitionistic fuzzy g -closed in X
- (c) Intuitionistic fuzzy sg -continuous [19] if the pre image of every intuitionistic fuzzy closed set in Y is intuitionistic fuzzy sg -closed in X .
- (d) Intuitionistic fuzzy gs -continuous [12] if the pre image of every intuitionistic fuzzy closed set in Y is intuitionistic fuzzy gs -closed in X .

Remark 2.4[12, 16, 19]:

- (a) Every intuitionistic fuzzy continuous mapping is intuitionistic fuzzy g -continuous, but the converse may not be true [16].
- (b) Every intuitionistic fuzzy semi continuous mapping is intuitionistic fuzzy sg -continuous, but the converse may not be true [19].
- (c) Every intuitionistic fuzzy sg -continuous mapping is intuitionistic fuzzy gs -continuous, but the converse may not be true [12].
- (d) Every intuitionistic fuzzy g -continuous mapping is intuitionistic fuzzy gs -continuous, but the converse may not be true [12].

3. INTUITIONISTIC FUZZY W-CLOSED SET

Definition 3.1: An intuitionistic fuzzy set A of an intuitionistic fuzzy topological space (X, \mathfrak{S}) is called an intuitionistic fuzzy w -closed if $cl(A) \subseteq O$ whenever $A \subseteq O$ and O is intuitionistic fuzzy semi open.

Remark 3.1: Every intuitionistic fuzzy closed set is intuitionistic fuzzy w -closed but its converse may not be true.

Example 3.1: Let $X = \{a, b\}$ and $\mathfrak{S} = \{\tilde{0}, \tilde{1}, U\}$ be an intuitionistic fuzzy topology on X , where $U = \{ \langle a, 0.5, 0.5 \rangle, \langle b, 0.4, 0.6 \rangle \}$. Then the intuitionistic fuzzy set $A = \{ \langle a, 0.5, 0.5 \rangle, \langle b, 0.5, 0.5 \rangle \}$ is intuitionistic fuzzy w -closed but it is not intuitionistic fuzzy closed.

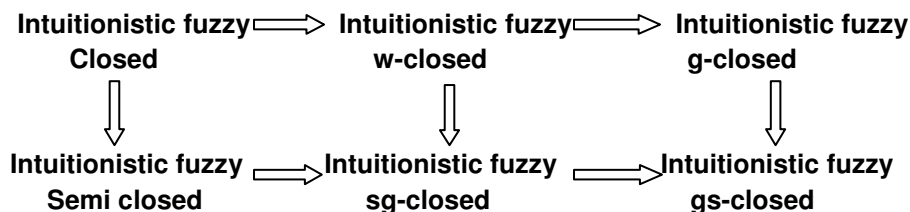
Remark 3.2: Every intuitionistic fuzzy w -closed set is intuitionistic fuzzy g -closed but its converse may not be true.

Example 3.2: Let $X = \{a, b\}$ and $\mathfrak{S} = \{\tilde{0}, \tilde{1}, U\}$ be an intuitionistic fuzzy topology on X , where $U = \{ \langle a, 0.7, 0.3 \rangle, \langle b, 0.6, 0.4 \rangle \}$. Then the intuitionistic fuzzy set $A = \{ \langle a, 0.6, 0.4 \rangle, \langle b, 0.7, 0.3 \rangle \}$ is intuitionistic fuzzy g -closed but it is not intuitionistic fuzzy w -closed.

Remark 3.3: Every intuitionistic fuzzy w -closed set is intuitionistic fuzzy sg -closed but its converse may not be true.

Example 3.3: Let $X = \{a, b\}$ and $\mathfrak{S} = \{\tilde{0}, \tilde{1}, U\}$ be an intuitionistic fuzzy topology on X , where $U = \{ \langle a, 0.5, 0.5 \rangle, \langle b, 0.4, 0.6 \rangle \}$. Then the intuitionistic fuzzy set $A = \{ \langle a, 0.5, 0.5 \rangle, \langle b, 0.3, 0.7 \rangle \}$ is intuitionistic fuzzy sg -closed but it is not intuitionistic fuzzy w -closed.

Remark 3.4: Remarks 2.1, 2.2, 2.3, 3.1, 3.2, 3.3 reveals the following diagram of implication.



Theorem 3.1: Let (X, \mathfrak{S}) be an intuitionistic fuzzy topological space and A is an intuitionistic fuzzy set of X . Then A is intuitionistic fuzzy w -closed if and only if $\neg(A_q F) \Rightarrow \neg(\text{cl}(A)_q F)$ for every intuitionistic fuzzy semi closed set F of X .

Proof: Necessity: Let F be an intuitionistic fuzzy semi closed set of X and $\neg(A_q F)$. Then by Lemma 2.1(a), $A \subseteq F^c$ and F^c intuitionistic fuzzy semi open in X . Therefore $\text{cl}(A) \subseteq F^c$ by Def 3.1 because A is intuitionistic fuzzy w -closed. Hence by lemma 2.1(a), $\neg(\text{cl}(A)_q F)$.

Sufficiency: Let O be an intuitionistic fuzzy semi open set of X such that $A \subseteq O$ i.e. $A \subseteq (O^c)^c$. Then by Lemma 2.1(a), $\neg(A_q O^c)$ and O^c is an intuitionistic fuzzy semi closed set in X . Hence by hypothesis $\neg(\text{cl}(A)_q O^c)$. Therefore by Lemma 2.1(a), $\text{cl}(A) \subseteq (O^c)^c$ i.e. $\text{cl}(A) \subseteq O$. Hence A is intuitionistic fuzzy w -closed in X .

Theorem 3.2: Let A be an intuitionistic fuzzy w -closed set in an intuitionistic fuzzy topological space (X, \mathfrak{S}) and $c(\alpha, \beta)$ be an intuitionistic fuzzy point of X such that $c(\alpha, \beta)_q \text{cl}(A)$ then $\text{cl}(c(\alpha, \beta))_q A$.

Proof: If $\neg \text{cl}(c(\alpha, \beta))_q A$ then by Lemma 2.1(a), $\text{cl}(c(\alpha, \beta)) \subseteq A^c$ which implies that $A \subseteq (\text{cl}(c(\alpha, \beta)))^c$ and so $\text{cl}(A) \subseteq (\text{cl}(c(\alpha, \beta)))^c \subseteq (c(\alpha, \beta))^c$, because A is intuitionistic fuzzy w -closed in X . Hence by Lemma 2.1(a), $\neg(c(\alpha, \beta)_q \text{cl}(A))$, a contradiction.

Theorem 3.3: Let A and B are two intuitionistic fuzzy w -closed sets in an intuitionistic fuzzy topological space (X, \mathfrak{S}) , then $A \cup B$ is intuitionistic fuzzy w -closed.

Proof: Let O be an intuitionistic fuzzy semi open set in X , such that $A \cup B \subseteq O$. Then $A \subseteq O$ and $B \subseteq O$. So, $\text{cl}(A) \subseteq O$ and $\text{cl}(B) \subseteq O$. Therefore $\text{cl}(A) \cup \text{cl}(B) = \text{cl}(A \cup B) \subseteq O$. Hence $A \cup B$ is intuitionistic fuzzy w -closed.

Remark 3.2: The intersection of two intuitionistic fuzzy w -closed sets in an intuitionistic fuzzy topological space (X, \mathfrak{S}) may not be intuitionistic fuzzy w -closed. For,

Example 3.2: Let $X = \{a, b, c\}$ and U, A and B be the intuitionistic fuzzy sets of X defined as follows:

$$\begin{aligned}
 U &= \{ \langle a, 1, 0 \rangle, \langle b, 0, 1 \rangle, \langle c, 0, 1 \rangle \} \\
 A &= \{ \langle a, 1, 0 \rangle, \langle b, 1, 0 \rangle, \langle c, 0, 1 \rangle \} \\
 B &= \{ \langle a, 1, 0 \rangle, \langle b, 0, 1 \rangle, \langle c, 1, 0 \rangle \}
 \end{aligned}$$

Let $\mathfrak{S} = \{\tilde{0}, \tilde{1}, U\}$ be intuitionistic fuzzy topology on X . Then A and B are intuitionistic fuzzy w -closed in (X, \mathfrak{S}) but $A \cap B$ is not intuitionistic fuzzy w -closed.

Theorem 3.4: Let A be an intuitionistic fuzzy w -closed set in an intuitionistic fuzzy topological space (X, \mathfrak{S}) and $A \subseteq B \subseteq cl(A)$. Then B is intuitionistic fuzzy w -closed in X .

Proof: Let O be an intuitionistic fuzzy semi open set such that $B \subseteq O$. Then $A \subseteq O$ and since A is intuitionistic fuzzy w -closed, $cl(A) \subseteq O$. Now $B \subseteq cl(A) \Rightarrow cl(B) \subseteq cl(A) \subseteq O$. Consequently B is intuitionistic fuzzy w -closed.

Definition 3.2: An intuitionistic fuzzy set A of an intuitionistic fuzzy topological space (X, \mathfrak{S}) is called intuitionistic fuzzy w -open if and only if its complement A^c is intuitionistic fuzzy w -closed.

Remark 3.5 Every intuitionistic fuzzy open set is intuitionistic fuzzy w -open. But the converse may not be true. For

Example 3.4: Let $X = \{a, b\}$ and $\mathfrak{S} = \{\tilde{0}, \tilde{1}, U\}$ be an intuitionistic fuzzy topology on X , where $U = \{ \langle a, 0.5, 0.5 \rangle, \langle b, 0.4, 0.6 \rangle \}$. Then intuitionistic fuzzy set B defined by $B = \{ \langle a, 0.5, 0.5 \rangle, \langle b, 0.5, 0.5 \rangle \}$ is an intuitionistic fuzzy w -open in intuitionistic fuzzy topological space (X, \mathfrak{S}) but it is not intuitionistic fuzzy open in (X, \mathfrak{S}) .

Remark 3.6: Every intuitionistic fuzzy w -open set is intuitionistic fuzzy g -open but its converse may not be true.

Example 3.5: Let $X = \{a, b\}$ and $\mathfrak{S} = \{\tilde{0}, \tilde{1}, U\}$ be an intuitionistic fuzzy topology on X , where $U = \{ \langle a, 0.5, 0.5 \rangle, \langle b, 0.4, 0.6 \rangle \}$. Then the intuitionistic fuzzy set $A = \{ \langle a, 0.4, 0.6 \rangle, \langle b, 0.3, 0.7 \rangle \}$ is intuitionistic fuzzy g -open in (X, \mathfrak{S}) but it is not intuitionistic fuzzy w -open in (X, \mathfrak{S}) .

Theorem 3.5: An intuitionistic fuzzy set A of an intuitionistic fuzzy topological space (X, \mathfrak{S}) is intuitionistic fuzzy w -open if $F \subseteq int(A)$ whenever F is intuitionistic fuzzy semi closed and $F \subseteq A$.

Proof: Follows from definition 3.1 and Lemma 2.1

Remark 3.4: The union of two intuitionistic fuzzy w -open sets in an intuitionistic fuzzy topological space (X, \mathfrak{S}) may not be intuitionistic fuzzy w -open. For the intuitionistic fuzzy set $C = \{ \langle a, 0.4, 0.6 \rangle, \langle b, 0.7, 0.3 \rangle \}$ and $D = \{ \langle a, 0.2, 0.8 \rangle, \langle b, 0.5, 0.5 \rangle \}$ in the intuitionistic fuzzy topological space (X, \mathfrak{S}) in Example 3.2 are intuitionistic fuzzy w -open but their union is not intuitionistic fuzzy w -open.

Theorem 3.6: Let A be an intuitionistic fuzzy w -open set of an intuitionistic fuzzy topological space (X, \mathfrak{S}) and $int(A) \subseteq B \subseteq A$. Then B is intuitionistic fuzzy w -open.

Proof: Suppose A is an intuitionistic fuzzy w -open in X and $int(A) \subseteq B \subseteq A \Rightarrow A^c \subseteq B^c \subseteq (int(A))^c \Rightarrow A^c \subseteq B^c \subseteq cl(A^c)$ by Lemma 2.1(d) and A^c is intuitionistic fuzzy w -closed it follows from theorem 3.4 that B^c is intuitionistic fuzzy w -closed. Hence B is intuitionistic fuzzy w -open.

Definition 3.3: An intuitionistic fuzzy topological space (X, \mathfrak{S}) is called intuitionistic fuzzy semi normal if for every pair of two intuitionistic fuzzy semi closed sets F_1 and F_2 such that $\bigcap(F_1, F_2)$, there exists two intuitionistic fuzzy semi open sets U_1 and U_2 in X such that $F_1 \subseteq U_1, F_2 \subseteq U_2$ and $\bigcap(U_1, U_2)$.

Theorem 3.7: If F is intuitionistic fuzzy semi closed and A is intuitionistic fuzzy w -closed set of an intuitionistic fuzzy semi normal space (X, \mathfrak{S}) and $\overline{\cap}(A)_q F$. Then there exists intuitionistic fuzzy semi open sets U and V in X such that $cl(A) \subseteq U$, $F \subseteq V$ and $\overline{\cap}(U \cap V)$.

Proof: Since A is intuitionistic fuzzy w -closed set and $\overline{\cap}(A)_q F$, by Theorem (3.1), $\overline{\cap}(cl(A))_q F$ and (X, \mathfrak{S}) is intuitionistic fuzzy semi normal. Therefore by Definition 3.3 there exists intuitionistic fuzzy semi open sets U and V in X such that $cl(A) \subseteq U$, $F \subseteq V$ and $\overline{\cap}(U \cap V)$.

Theorem 3.8: Let A be an intuitionistic fuzzy w -closed set in an intuitionistic fuzzy topological space (X, \mathfrak{S}) and $f: (X, \mathfrak{S}) \rightarrow (Y, \mathfrak{S}^*)$ is an intuitionistic fuzzy irresolute and intuitionistic fuzzy closed mapping then $f(A)$ is an intuitionistic w -closed set in Y .

Proof: Let A be an intuitionistic fuzzy w -closed set in X and $f: (X, \mathfrak{S}) \rightarrow (Y, \mathfrak{S}^*)$ is an intuitionistic fuzzy continuous and intuitionistic fuzzy closed mapping. Let $f(A) \subseteq G$ where G is intuitionistic fuzzy semi open in Y then $A \subseteq f^{-1}(G)$ and $f^{-1}(G)$ is intuitionistic fuzzy semi open in X because f is intuitionistic fuzzy irresolute. Now A be an intuitionistic fuzzy w -closed set in X , by definition 3.1 $cl(A) \subseteq f^{-1}(G)$. Thus $f(cl(A)) \subseteq G$ and $f(cl(A))$ is an intuitionistic fuzzy closed set in Y (since $cl(A)$ is intuitionistic fuzzy closed in X and f is intuitionistic fuzzy closed mapping). It follows that $cl(f(A)) \subseteq cl(f(cl(A))) = f(cl(A)) \subseteq G$. Hence $cl(f(A)) \subseteq G$ whenever $f(A) \subseteq G$ and G is intuitionistic fuzzy semi open in Y . Hence $f(A)$ is intuitionistic fuzzy w -closed set in Y .

Theorem 3.9: Let (X, \mathfrak{S}) be an intuitionistic fuzzy topological space and $IFSO(X)$ (resp. $IFC(X)$) be the family of all intuitionistic fuzzy semi open (resp. intuitionistic fuzzy closed) sets of X . Then $IFSO(X) = IFC(X)$ if and only if every intuitionistic fuzzy set of X is intuitionistic fuzzy w -closed.

Proof :Necessity : Suppose that $IFSO(X) = IFC(X)$ and let A is any intuitionistic fuzzy set of X such that $A \subseteq U \in IFSO(X)$ i.e. U is intuitionistic fuzzy semi open. Then $cl(A) \subseteq cl(U) = U$ because $U \in IFSO(X) = IFC(X)$. Hence $cl(A) \subseteq U$ whenever $A \subseteq U$ and U is intuitionistic fuzzy semi open. Hence A is w -closed set.

Sufficiency: Suppose that every intuitionistic fuzzy set of X is intuitionistic fuzzy w -closed. Let $U \in IFSO(X)$ then since $U \subseteq U$ and U is intuitionistic fuzzy w -closed, $cl(U) \subseteq U$ then $U \in IFC(X)$. Thus $IFSO(X) \subseteq IFC(X)$. If $T \in IFC(X)$ then $T^c \in IFO(X) \subseteq IFSO \subseteq IFC(X)$ hence $T \in IFO(X) \subseteq IFSO(X)$. Consequently $IFC(X) \subseteq IFSO(X)$ and $IFSO(X) = IFC(X)$.

4: INTUITIONISTIC FUZZY W-CONNECTEDNESS AND INTUITIONISTIC FUZZY W-COMPACTNESS

Definition 4.1: An intuitionistic fuzzy topological space (X, \mathfrak{S}) is called intuitionistic fuzzy w -connected if there is no proper intuitionistic fuzzy set of X which is both intuitionistic fuzzy w -open and intuitionistic fuzzy w -closed.

Theorem 4.1: Every intuitionistic fuzzy w -connected space is intuitionistic fuzzy connected.

Proof: Let (X, \mathfrak{S}) be an intuitionistic fuzzy w -connected space and suppose that (X, \mathfrak{S}) is not intuitionistic fuzzy connected. Then there exists a proper intuitionistic fuzzy set A ($A \neq \mathbf{0}, A \neq \mathbf{1}$) such that A is both

intuitionistic fuzzy open and intuitionistic fuzzy closed. Since every intuitionistic fuzzy open set (resp. intuitionistic fuzzy closed set) is intuitionistic w-open ((resp. intuitionistic fuzzy w-closed), X is not intuitionistic fuzzy w-connected, a contradiction.

Remark 4.1: Converse of theorem 4.1 may not be true for ,

Example 4.1: Let $X = \{a, b\}$ and $\mathfrak{S} = \{\tilde{0}, \tilde{1}, U\}$ be an intuitionistic fuzzy topology on X, where $U = \{< a, 0.5, 0.5>, < b, 0.4, 0.6 > \}$. Then intuitionistic fuzzy topological space (X, \mathfrak{S}) is intuitionistic fuzzy connected but not intuitionistic fuzzy w-connected because there exists a proper intuitionistic fuzzy set $A = \{< a, 0.5, 0.5>, < b, 0.5, 0.5>\}$ which is both intuitionistic fuzzy w-closed and intuitionistic w-open in X.

Theorem 4.2: An intuitionistic fuzzy topological (X, \mathfrak{S}) is intuitionistic fuzzy w-connected if and only if there exists no non zero intuitionistic fuzzy w-open sets A and B in X such that $A = B^c$.

Proof: Necessity: Suppose that A and B are intuitionistic fuzzy w-open sets such that $A \neq \tilde{0} \neq B$ and $A = B^c$. Since $A = B^c$, B is an intuitionistic fuzzy w-open set which implies that $B^c = A$ is intuitionistic fuzzy w-closed set and $B \neq \tilde{0}$ this implies that $B^c \neq \tilde{1}$ i.e. $A \neq \tilde{1}$ Hence there exists a proper intuitionistic fuzzy set $A (A \neq \tilde{0}, A \neq \tilde{1})$ such that A is both intuitionistic fuzzy w-open and intuitionistic fuzzy w-closed. But this is contradiction to the fact that X is intuitionistic fuzzy w-connected.

Sufficiency: Let (X, \mathfrak{S}) is an intuitionistic fuzzy topological space and A is both intuitionistic fuzzy w-open set and intuitionistic fuzzy w-closed set in X such that $\tilde{0} \neq A \neq \tilde{1}$. Now take $B = A^c$. In this case B is an intuitionistic fuzzy w-open set and $A \neq \tilde{1}$. This implies that $B = A^c \neq \tilde{0}$ which is a contradiction. Hence there is no proper intuitionistic fuzzy set of X which is both intuitionistic fuzzy w-open and intuitionistic fuzzy w-closed. Therefore intuitionistic fuzzy topological (X, \mathfrak{S}) is intuitionistic fuzzy w-connected

Definition 4.2: Let (X, \mathfrak{S}) be an intuitionistic fuzzy topological space and A be an intuitionistic fuzzy set X. Then w-interior and w-closure of A are defined as follows.

$$\begin{aligned} \text{wcl}(A) &= \bigcap \{K: K \text{ is an intuitionistic fuzzy w-closed set in } X \text{ and } A \subseteq K\} \\ \text{wint}(A) &= \bigcup \{G: G \text{ is an intuitionistic fuzzy w-open set in } X \text{ and } G \subseteq A\} \end{aligned}$$

Theorem 4.3: An intuitionistic fuzzy topological space (X, \mathfrak{S}) is intuitionistic fuzzy w-connected if and only if there exists no non zero intuitionistic fuzzy w-open sets A and B in X such that $B = A^c, B = (\text{wcl}(A))^c, A = (\text{wcl}(B))^c$.

Proof: Necessity : Assume that there exists intuitionistic fuzzy sets A and B such that $A \neq \tilde{0} \neq B$ in X such that $B = A^c, B = (\text{wcl}(A))^c, A = (\text{wcl}(B))^c$. Since $(\text{wcl}(A))^c$ and $(\text{wcl}(B))^c$ are intuitionistic fuzzy w-open sets in X, which is a contradiction.

Sufficiency: Let A is both an intuitionistic fuzzy w-open set and intuitionistic fuzzy w-closed set such that $\tilde{0} \neq A \neq \tilde{1}$. Taking $B = A^c$, we obtain a contradiction.

Definition 4.3: An intuitionistic fuzzy topological space (X, \mathfrak{S}) is said to be intuitionistic fuzzy w- $T_{1/2}$ if every intuitionistic fuzzy w-closed set in X is intuitionistic fuzzy closed in X.

Theorem 4.4: Let (X, \mathfrak{S}) be an intuitionistic fuzzy w- $T_{1/2}$ space, then the following conditions are equivalent:

- (a) X is intuitionistic fuzzy w-connected.

(b) X is intuitionistic fuzzy connected.

Proof: (a) \Rightarrow (b) follows from Theorem 4.1

(b) \Rightarrow (a): Assume that X is intuitionistic fuzzy w - $T_{1/2}$ and intuitionistic fuzzy w -connected space. If possible, let X be not intuitionistic fuzzy w -connected, then there exists a proper intuitionistic fuzzy set A such that A is both intuitionistic fuzzy w -open and w -closed. Since X is intuitionistic fuzzy w - $T_{1/2}$, A is intuitionistic fuzzy open and intuitionistic fuzzy closed which implies that X is not intuitionistic fuzzy connected, a contradiction.

Definition 4.4 : A collection $\{ A_i : i \in \Lambda \}$ of intuitionistic fuzzy w - open sets in intuitionistic fuzzy topological space (X, \mathfrak{S}) is called intuitionistic fuzzy w - open cover of intuitionistic fuzzy set B of X if $B \subseteq \cup \{ A_i : i \in \Lambda \}$

Definition 4.5: An intuitionistic fuzzy topological space (X, \mathfrak{S}) is said to be intuitionistic fuzzy w -compact if every intuitionistic fuzzy w - open cover of X has a finite sub cover.

Definition 4.6 : An intuitionistic fuzzy set B of intuitionistic fuzzy topological space (X, \mathfrak{S}) is said to be intuitionistic fuzzy w - compact relative to X , if for every collection $\{ A_i : i \in \Lambda \}$ of intuitionistic fuzzy w - open subset of X such that $B \subseteq \cup \{ A_i : i \in \Lambda \}$ there exists finite subset Λ_0 of Λ such that $B \subseteq \cup \{ A_i : i \in \Lambda_0 \}$

Definition 4.7: A crisp subset B of intuitionistic fuzzy topological space (X, \mathfrak{S}) is said to be intuitionistic fuzzy w - compact if B is intuitionistic fuzzy w - compact as intuitionistic fuzzy subspace of X .

Theorem 4.5: A intuitionistic fuzzy w -closed crisp subset of intuitionistic fuzzy w - compact space is intuitionistic fuzzy w - compact relative to X .

Proof: Let A be an intuitionistic fuzzy w - closed crisp subset of intuitionistic fuzzy w - compact space (X, \mathfrak{S}) . Then A^c is intuitionistic fuzzy w - open in X . Let M be a cover of A by intuitionistic fuzzy w - open sets in X . Then the family $\{M, A^c\}$ is intuitionistic fuzzy w - open cover of X . Since X is intuitionistic fuzzy w - compact, it has a finite sub cover say $\{G_1, G_2, G_3, \dots, G_n\}$. If this sub cover contains A^c , we discard it. Otherwise leave the sub cover as it is. Thus we obtained a finite intuitionistic fuzzy w – open sub cover of A . Therefore A is intuitionistic fuzzy w – compact relative to X .

5: INTUITIONISTIC FUZZY W- CONTINUOUS MAPPINGS

Definition 5.1: A mapping $f : (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w - continuous if inverse image of every intuitionistic fuzzy closed set of Y is intuitionistic fuzzy w -closed set in X .

Theorem 5.1: A mapping $f : (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w - continuous if and only if the inverse image of every intuitionistic fuzzy open set of Y is intuitionistic fuzzy w - open in X .

Proof: It is obvious because $f^{-1}(U^c) = (f^{-1}(U))^c$ for every intuitionistic fuzzy set U of Y .

Remark5.1 Every intuitionistic fuzzy continuous mapping is intuitionistic fuzzy w -continuous, but converse may not be true. For,

Example 5.1 Let $X = \{a, b\}$, $Y = \{x, y\}$ and intuitionistic fuzzy sets U and V are defined as follows :

$U = \{ \langle a, 0.5, 0.5 \rangle, \langle b, 0.4, 0.6 \rangle \}$

$V = \{ \langle x, 0.5, 0.5 \rangle, \langle y, 0.5, 0.5 \rangle \}$

Let $\mathfrak{S} = \{\tilde{0}, \tilde{1}, \mathbf{U}\}$ and $\sigma = \{\tilde{0}, \tilde{1}, \mathbf{V}\}$ be intuitionistic fuzzy topologies on X and Y respectively. Then the mapping $f: (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ defined by $f(a) = x$ and $f(b) = y$ is intuitionistic fuzzy w -continuous but not intuitionistic fuzzy continuous.

Remark5.2 Every intuitionistic fuzzy w -continuous mapping is intuitionistic fuzzy g -continuous, but converse may not be true. For,

Example 5.2: Let $X = \{a, b\}$, $Y = \{x, y\}$ and intuitionistic fuzzy sets U and V are defined as follows:

$$U = \{ \langle a, 0.7, 0.3 \rangle, \langle b, 0.6, 0.4 \rangle \}$$

$$V = \{ \langle x, 0.6, 0.4 \rangle, \langle y, 0.7, 0.3 \rangle \}$$

Let $\mathfrak{S} = \{ \tilde{0}, \tilde{1}, \mathbf{U} \}$ and $\sigma = \{ \tilde{0}, \tilde{1}, \mathbf{V} \}$ be intuitionistic fuzzy topologies on X and Y respectively. Then the mapping $f: (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ defined by $f(a) = x$ and $f(b) = y$ is intuitionistic fuzzy g -continuous but not intuitionistic fuzzy w -continuous.

Remark5.3 Every intuitionistic fuzzy w -continuous mapping is intuitionistic fuzzy sg -continuous, but converse may not be true. For,

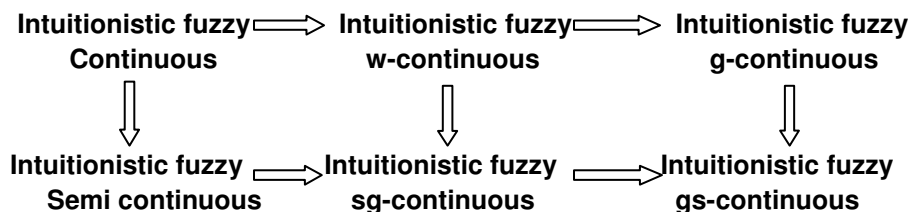
Example 5.1 Let $X = \{a, b\}$, $Y = \{x, y\}$ and intuitionistic fuzzy sets U and V are defined as follows:

$$U = \{ \langle a, 0.5, 0.5 \rangle, \langle b, 0.4, 0.6 \rangle \}$$

$$V = \{ \langle x, 0.5, 0.5 \rangle, \langle y, 0.3, 0.7 \rangle \}$$

Let $\mathfrak{S} = \{ \tilde{0}, \tilde{1}, \mathbf{U} \}$ and $\sigma = \{ \tilde{0}, \tilde{1}, \mathbf{V} \}$ be intuitionistic fuzzy topologies on X and Y respectively. Then the mapping $f: (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ defined by $f(a) = x$ and $f(b) = y$ is intuitionistic fuzzy sg -continuous but not intuitionistic fuzzy w -continuous.

Remark 5.4: Remarks 2.4, 5.1, 5.2, 5.3 reveals the following diagram of implication:



Theorem 5.2: If $f: (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w -continuous then for each intuitionistic fuzzy point $c(\alpha, \beta)$ of X and each intuitionistic fuzzy open set V of Y such that $f(c(\alpha, \beta)) \subseteq V$ there exists a intuitionistic fuzzy w -open set U of X such that $c(\alpha, \beta) \subseteq U$ and $f(U) \subseteq V$.

Proof : Let $c(\alpha, \beta)$ be intuitionistic fuzzy point of X and V be a intuitionistic fuzzy open set of Y such that $f(c(\alpha, \beta)) \subseteq V$. Put $U = f^{-1}(V)$. Then by hypothesis U is intuitionistic fuzzy w -open set of X such that $c(\alpha, \beta) \subseteq U$ and $f(U) = f(f^{-1}(V)) \subseteq V$.

Theorem 5.3: Let $f: (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w -continuous then for each intuitionistic fuzzy point $c(\alpha, \beta)$ of X and each intuitionistic fuzzy open set V of Y such that $f(c(\alpha, \beta)) \not\subseteq V$, there exists a intuitionistic fuzzy w -open set U of X such that $c(\alpha, \beta) \not\subseteq U$ and $f(U) \subseteq V$.

Proof: Let $c(\alpha, \beta)$ be intuitionistic fuzzy point of X and V be a intuitionistic fuzzy open set of Y such that $f(c(\alpha, \beta)) \not\subseteq V$. Put $U = f^{-1}(V)$. Then by hypothesis U is intuitionistic fuzzy w -open set of X such that $c(\alpha, \beta) \not\subseteq U$ and $f(U) = f(f^{-1}(V)) \subseteq V$.

Theorem 5.4: If $f : (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w-continuous, then $f(\text{wcl}(A)) \subseteq \text{cl}(f(A))$ for every intuitionistic fuzzy set A of X.

Proof: Let A be an intuitionistic fuzzy set of X. Then $\text{cl}(f(A))$ is an intuitionistic fuzzy closed set of Y. Since f is intuitionistic fuzzy w –continuous, $f^{-1}(\text{cl}(f(A)))$ is intuitionistic fuzzy w-closed in X. Clearly $A \subseteq f^{-1}(\text{cl}(f(A)))$. Therefore $\text{wcl}(A) \subseteq \text{wcl}(f^{-1}(\text{cl}(f(A)))) = f^{-1}(\text{cl}(f(A)))$. Hence $f(\text{wcl}(A)) \subseteq \text{cl}(f(A))$ for every intuitionistic fuzzy set A of X.

Theorem 5.5: A mapping f from an intuitionistic fuzzy w- $T_{1/2}$ space (X, \mathfrak{S}) to a intuitionistic fuzzy topological space (Y, σ) is intuitionistic fuzzy semi continuous if and only if it is intuitionistic fuzzy w – continuous.

Proof: Obvious

Remark 5.5: The composition of two intuitionistic fuzzy w – continuous mapping may not be Intuitionistic fuzzy w – continuous. For

Example 5-5: Let $X = \{a, b\}$, $Y = \{x, y\}$ and $Z = \{p, q\}$ and intuitionstic fuzzy sets U,V and W defined as follows :

$$U = \{ \langle a, 0.5, 0.5 \rangle, \langle b, 0.4, 0.6 \rangle \}$$

$$V = \{ \langle x, 0.5, 0.5 \rangle, \langle y, 0.3, 0.7 \rangle \}$$

$$W = \{ \langle p, 0.6, 0.4 \rangle, \langle q, 0.4, 0.6 \rangle \}$$

Let $\mathfrak{S} = \{ \tilde{0}, \tilde{1}, U \}$, $\sigma = \{ \tilde{0}, \tilde{1}, V \}$ and $\mu = \{ \tilde{0}, \tilde{1}, W \}$ be intuitionistic fuzzy topologies on X , Y and Z respectively. Let the mapping $f : (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ defined by $f(a) = x$ and $f(b) = y$ and $g : (Y, \sigma) \rightarrow (Z, \mu)$ defined by $g(x) = p$ and $g(y) = q$. Then the mappings f and g are intuitionistic fuzzy w-continuous but the mapping $g \circ f : (X, \mathfrak{S}) \rightarrow (Z, \mu)$ is not intuitionistic fuzzy w-continuous.

Theorem 5.6: If $f : (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w-continuous and $g : (Y, \sigma) \rightarrow (Z, \mu)$ is intuitionistic fuzzy continuous. Then $g \circ f : (X, \mathfrak{S}) \rightarrow (Z, \mu)$ is intuitionistic fuzzy w-continuous.

Proof: Let A is an intuitionistic fuzzy closed set in Z. then $g^{-1}(A)$ is intuitionstic fuzzy closed in Y because g is intuitionistic fuzzy continuous. Therefore $(g \circ f)^{-1}(A) = f^{-1}(g^{-1}(A))$ is intuitionistic fuzzy w – closed in X. Hence $g \circ f$ is intuitionistic fuzzy w –continuous.

Theorem 5.7 : If $f : (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w-continuous and $g : (Y, \sigma) \rightarrow (Z, \mu)$ is intuitionistic fuzzy g-continuous and (Y, σ) is intuitionistic fuzzy $(T_{1/2})$ then $g \circ f : (X, \mathfrak{S}) \rightarrow (Z, \mu)$ is intuitionistic fuzzy w-continuous.

Proof: Let A is an intuitionistic fuzzy closed set in Z, then $g^{-1}(A)$ is intuitionstic fuzzy g-closed in Y. Since Y is $(T_{1/2})$, then $g^{-1}(A)$ is intuitionstic fuzzy closed in Y. Hence $(g \circ f)^{-1}(A) = f^{-1}(g^{-1}(A))$ is intuitionistic fuzzy w – closed in X. Hence $g \circ f$ is intuitionistic fuzzy w – continuous.

Theorem 5.8: If $f : (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy gc-irresolute and $g : (Y, \sigma) \rightarrow (Z, \mu)$ is intuitionistic fuzzy w-continuous. Then $g \circ f : (X, \mathfrak{S}) \rightarrow (Z, \mu)$ is intuitionistic fuzzy g-continuous.

Proof: Let A is an intuitionistic fuzzy closed set in Z, then $g^{-1}(A)$ is intuitionstic fuzzy w-closed in Y, because g is intuitionistic fuzzy w-continuous. Since every intuitionistic fuzzy w-closed set is intuitionistic fuzzy g-closed set, therefore $g^{-1}(A)$ is intuitionstic fuzzy g-closed in Y .Then $(g \circ f)^{-1}(A) = f^{-1}(g^{-1}(A))$ is intuitionistic fuzzy g-closed in X ,because f is intuitionistic fuzzy gc- irresolute. Hence $g \circ f : (X, \mathfrak{S}) \rightarrow (Z, \mu)$ is intuitionistic fuzzy g-continuous.

Theorem 5.9: An intuitionistic fuzzy w – continuous image of a intuitionistic fuzzy w-compact space is intuitionistic fuzzy compact.

Proof: Let. $f: (X, \mathfrak{S}). \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w-continuous map from a intuitionistic fuzzy w-compact space (X, \mathfrak{S}) onto a intuitionistic fuzzy topological space (Y, σ) . Let $\{A_i: i \in \Lambda\}$ be an intuitionistic fuzzy open cover of Y then $\{f^{-1}(A_i) : i \in \Lambda\}$ is a intuitionistic fuzzy w-open cover of X . Since X is intuitionistic fuzzy w-compact it has finite intuitionistic fuzzy sub cover say $\{f^{-1}(A_1), f^{-1}(A_2), \dots, f^{-1}(A_n)\}$. Since f is onto $\{A_1, A_2, \dots, A_n\}$ is an intuitionistic fuzzy open cover of Y and so (Y, σ) is intuitionistic fuzzy compact.

Theorem 5.10: If $f: (X, \mathfrak{S}). \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w-continuous surjection and X is intuitionistic fuzzy w-connected then Y is intuitionistic fuzzy connected.

Proof: Suppose Y is not intuitionistic fuzzy connected. Then there exists a proper intuitionistic fuzzy set G of Y which is both intuitionistic fuzzy open and intuitionistic fuzzy closed. Therefore $f^{-1}(G)$ is a proper intuitionistic fuzzy set of X , which is both intuitionistic fuzzy w-open and intuitionistic fuzzy w-closed, because f is intuitionistic fuzzy w-continuous surjection. Hence X is not intuitionistic fuzzy w-connected, which is a contradiction.

6. INTUITIONISTIC FUZZY W-OPEN MAPPINGS

Definition 6.1: A mapping $f: (X, \mathfrak{S}). \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w-open if the image of every intuitionistic fuzzy open set of X is intuitionistic fuzzy w-open set in Y .

Remark 6.1 : Every intuitionistic fuzzy open map is intuitionistic fuzzy w-open but converse may not be true. For,

Example 6.1: Let $X = \{a, b\}$, $Y = \{x, y\}$ and the intuitionistic fuzzy set U and V are defined as follows :

$$U = \{ \langle a, 0.5, 0.5 \rangle, \langle b, 0.4, 0.6 \rangle \}$$

$$V = \{ \langle x, 0.5, 0.5 \rangle, \langle y, 0.3, 0.7 \rangle \}$$

Then $\mathfrak{S} = \{ \tilde{0}, U, \tilde{1} \}$ and $\sigma = \{ \tilde{0}, V, \tilde{1} \}$ be intuitionistic fuzzy topologies on X and Y respectively. Then the mapping $f: (X, \mathfrak{S}). \rightarrow (Y, \sigma)$ defined by $f(a) = x$ and $f(b) = y$ is intuitionistic fuzzy w-open but it is not intuitionistic fuzzy open.

Theorem 6.1: A mapping $f: (X, \mathfrak{S}). \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w-open if and only if for every intuitionistic fuzzy set U of X $f(\text{int}(U)) \subseteq \text{wint}(f(U))$.

Proof: Necessity Let f be an intuitionistic fuzzy w-open mapping and U is an intuitionistic fuzzy open set in X . Now $\text{int}(U) \subseteq U$ which implies that $f(\text{int}(U)) \subseteq f(U)$. Since f is an intuitionistic fuzzy w-open mapping, $f(\text{int}(U))$ is intuitionistic fuzzy w-open set in Y such that $f(\text{int}(U)) \subseteq f(U)$ therefore $f(\text{int}(U)) \subseteq \text{wint}(f(U))$.

Sufficiency: For the converse suppose that U is an intuitionistic fuzzy open set of X . Then $f(U) = f(\text{int}(U) \cup (U - \text{int}(U))) \subseteq \text{wint}(f(U)) \cup f(U - \text{int}(U))$. But $\text{wint}(f(U)) \subseteq f(U)$. Consequently $f(U) = \text{wint}(f(U))$ which implies that $f(U)$ is an intuitionistic fuzzy w-open set of Y and hence f is an intuitionistic fuzzy w-open.

Theorem 6.2: If $f: (X, \mathfrak{S}). \rightarrow (Y, \sigma)$ is an intuitionistic fuzzy w-open map then $\text{int}(f^{-1}(G)) \subseteq f^{-1}(\text{wint}(G))$ for every intuitionistic fuzzy set G of Y .

Proof: Let G is an intuitionistic fuzzy set of Y . Then $\text{int}(f^{-1}(G))$ is an intuitionistic fuzzy open set in X . Since f is intuitionistic fuzzy w-open $f(\text{int}(f^{-1}(G)))$ is intuitionistic fuzzy w-open in Y and hence $f(\text{int}(f^{-1}(G))) \subseteq \text{wint}(f(f^{-1}(G))) \subseteq \text{wint}(G)$. Thus $\text{int}(f^{-1}(G)) \subseteq f^{-1}(\text{wint}(G))$.

Theorem 6.3: A mapping $f : (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w-open if and only if for each intuitionistic fuzzy set S of Y and for each intuitionistic fuzzy closed set U of X containing $f^{-1}(S)$ there is an intuitionistic fuzzy w-closed V of Y such that $S \subseteq V$ and $f^{-1}(V) \subseteq U$.

Proof: Necessity: Suppose that f is an intuitionistic fuzzy w-open map. Let S be the intuitionistic fuzzy closed set of Y and U is an intuitionistic fuzzy closed set of X such that $f^{-1}(S) \subseteq U$. Then $V = (f^{-1}(U^c))^c$ is intuitionistic fuzzy w-closed set of Y such that $f^{-1}(V) \subseteq U$.

Sufficiency: For the converse suppose that F is an intuitionistic fuzzy open set of X . Then $f^{-1}((f(F))^c) \subseteq F^c$ and F^c is intuitionistic fuzzy closed set in X . By hypothesis there is an intuitionistic fuzzy w-closed set V of Y such that $(f(F))^c \subseteq V$ and $f^{-1}(V) \subseteq F^c$. Therefore $F \subseteq (f^{-1}(V))^c$. Hence $V^c \subseteq f(F) \subseteq f((f^{-1}(V))^c) \subseteq V^c$ which implies $f(F) = V^c$. Since V^c is intuitionistic fuzzy w-open set of Y . Hence $f(F)$ is intuitionistic fuzzy w-open in Y and thus f is intuitionistic fuzzy w-open map.

Theorem 6.4: A mapping $f : (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w-open if and only if $f^{-1}(wcl(B)) \subseteq cl f^{-1}(B)$ for every intuitionistic fuzzy set B of Y .

Proof: Necessity: Suppose that f is an intuitionistic fuzzy w-open map. For any intuitionistic fuzzy set B of Y $f^{-1}(B) \subseteq cl(f^{-1}(B))$. Therefore by theorem 6.3 there exists an intuitionistic fuzzy w-closed set F in Y such that $B \subseteq F$ and $f^{-1}(F) \subseteq cl(f^{-1}(B))$. Therefore we obtain that $f^{-1}(wcl(B)) \subseteq f^{-1}(F) \subseteq cl f^{-1}(B)$.

Sufficiency: For the converse suppose that B is an intuitionistic fuzzy set of Y . and F is an intuitionistic fuzzy closed set of X containing $f^{-1}(B)$. Put $V = cl(B)$, then we have $B \subseteq V$ and V is w-closed and $f^{-1}(V) \subseteq cl(f^{-1}(B)) \subseteq F$. Then by theorem 6.3 f is intuitionistic fuzzy w-open.

Theorem 6.5: If $f : (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ and $g : (Y, \sigma) \rightarrow (Z, \mu)$ be two intuitionistic fuzzy map and $gof : (X, \mathfrak{S}) \rightarrow (Z, \mu)$ is intuitionistic fuzzy w-open. If $g : (Y, \sigma) \rightarrow (Z, \mu)$ is intuitionistic fuzzy w-irresolute then $f : (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w-open map.

Proof: Let H be an intuitionistic fuzzy open set of intuitionistic fuzzy topological space (X, \mathfrak{S}) . Then $(gof)(H)$ is intuitionistic fuzzy w-open set of Z because gof is intuitionistic fuzzy w-open map. Now since $g : (Y, \sigma) \rightarrow (Z, \mu)$ is intuitionistic fuzzy w-irresolute and $(gof)(H)$ is intuitionistic fuzzy w-open set of Z therefore $g^{-1}((gof)(H)) = f(H)$ is intuitionistic fuzzy w-open set in intuitionistic fuzzy topological space Y . Hence f is intuitionistic fuzzy w-open map.

7. INTUITIONISTIC FUZZY W-CLOSED MAPPINGS

Definition 7.1: A mapping $f : (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w-closed if image of every intuitionistic fuzzy closed set of X is intuitionistic fuzzy w-closed set in Y .

Remark 7.1 Every intuitionistic fuzzy closed map is intuitionistic fuzzy w-closed but converse may not be true. For,

Example 7.1: Let $X = \{a, b\}$, $Y = \{x, y\}$

Then the mapping $f : (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ defined in Example 6.1 is intuitionistic fuzzy w-closed but it is not intuitionistic fuzzy closed.

Theorem 7.1: A mapping $f : (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w-closed if and only if for each intuitionistic fuzzy set S of Y and for each intuitionistic fuzzy open set U of X containing $f^{-1}(S)$ there is an intuitionistic fuzzy w-open set V of Y such that $S \subseteq V$ and $f^{-1}(V) \subseteq U$.

Proof: Necessity: Suppose that f is an intuitionistic fuzzy w - closed map. Let S be the intuitionistic fuzzy closed set of Y and U is an intuitionistic fuzzy open set of X such that $f^{-1}(S) \subseteq U$. Then $V = Y - f^{-1}(U^c)$ is intuitionistic fuzzy w - open set of Y such that $f^{-1}(V) \subseteq U$.

Sufficiency: For the converse suppose that F is an intuitionistic fuzzy closed set of X . Then $(f(F))^c$ is an intuitionistic fuzzy set of Y and F^c is intuitionistic fuzzy open set in X such that $f^{-1}((f(F))^c) \subseteq F^c$. By hypothesis there is an intuitionistic fuzzy w -open set V of Y such that $(f(F))^c \subseteq V$ and $f^{-1}(V) \subseteq F^c$. Therefore $F \subseteq (f^{-1}(V))^c$. Hence $V^c \subseteq f(F) \subseteq f((f^{-1}(V))^c) \subseteq V^c$ which implies $f(F) = V^c$. Since V^c is intuitionistic fuzzy w -closed set of Y . Hence $f(F)$ is intuitionistic fuzzy w -closed in Y and thus f is intuitionistic fuzzy w -closed map.

Theorem 7.2: If $f: (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy semi continuous and intuitionistic fuzzy w -closed map and A is an intuitionistic fuzzy w -closed set of X , then $f(A)$ intuitionistic fuzzy w -closed.

Proof: Let $f(A) \subseteq O$ where O is an intuitionistic fuzzy semi open set of Y . Since f is intuitionistic fuzzy semi continuous therefore $f^{-1}(O)$ is an intuitionistic fuzzy semi open set of X such that $A \subseteq f^{-1}(O)$. Since A is intuitionistic fuzzy w -closed of X which implies that $cl(A) \subseteq (f^{-1}(O))$ and hence $f(cl(A)) \subseteq O$ which implies that $cl(f(cl(A))) \subseteq O$ therefore $cl(f(A)) \subseteq O$ whenever $f(A) \subseteq O$ where O is an intuitionistic fuzzy semi open set of Y . Hence $f(A)$ is an intuitionistic fuzzy w -closed set of Y .

Corollary 7.1: If $f: (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy w -continuous and intuitionistic fuzzy closed map and A is an intuitionistic fuzzy w -closed set of X , then $f(A)$ intuitionistic fuzzy w -closed.

Theorem 7.3: If $f: (X, \mathfrak{S}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy closed and $g: (Y, \sigma) \rightarrow (Z, \mu)$ is intuitionistic fuzzy w -closed. Then $g \circ f: (X, \mathfrak{S}) \rightarrow (Z, \mu)$ is intuitionistic fuzzy w -closed.

Proof: Let H be an intuitionistic fuzzy closed set of intuitionistic fuzzy topological space (X, \mathfrak{S}) . Then $f(H)$ is intuitionistic fuzzy closed set of (Y, σ) because f is intuitionistic fuzzy closed map. Now $(g \circ f)(H) = g(f(H))$ is intuitionistic fuzzy w -closed set in intuitionistic fuzzy topological space Z because g is intuitionistic fuzzy w -closed map. Thus $g \circ f: (X, \mathfrak{S}) \rightarrow (Z, \mu)$ is intuitionistic fuzzy w -closed.

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